

# Package: gdverse (via r-universe)

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<i>cpsd_disc</i>	<i>optimal spatial data discretization based on SPADE q-statistics</i>
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## Description

Function for determining the optimal spatial data discretization based on SPADE q-statistics.

## Usage

```
cpsd_disc(
  formula,
  data,
  wt,
  discnum = NULL,
  discmethod = NULL,
  strategy = 2L,
  increase_rate = 0.05,
  cores = 1,
  return_disc = TRUE,
  seed = 123456789,
  ...
)
```

## Arguments

<b>formula</b>	A formula of optimal spatial data discretization.
<b>data</b>	A data.frame or tibble of observation data.
<b>wt</b>	The spatial weight matrix.
<b>discnum</b>	(optional) A vector of number of classes for discretization. Default is 3:22.
<b>discmethod</b>	(optional) A vector of methods for discretization, default is all using quantilein gdverse. see method parameter in <code>st_unidisc()</code> for more details.
<b>strategy</b>	(optional) Discretization strategy. When <code>strategy</code> is 1L, choose the highest SPADE model q-statistics to determinate optimal spatial data discretization parameters. When <code>strategy</code> is 2L, The optimal discrete parameters of spatial data are selected by combining LOESS model.
<b>increase_rate</b>	(optional) The critical increase rate of the number of discretization. Default is 5%.

<code>cores</code>	(optional) A positive integer(default is 1). If <code>cores &gt; 1</code> , a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
<code>return_disc</code>	(optional) Whether or not return discretized result used the optimal parameter. Default is TRUE.
<code>seed</code>	(optional) Random seed number, default is 123456789. Setting random seed is useful when the sample size is greater than 3000(the default value for <code>largeN</code> ) and the data is discretized by sampling 10%(the default value for <code>samp_prop</code> in <code>st_unidisc()</code> ).
<code>...</code>	(optional) Other arguments passed to <code>st_unidisc()</code> .

### Value

A list with the optimal parameter in the provided parameter combination with `k`, `method` and `disc`(when `return_disc` is TRUE).

### Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

### References

Yongze Song & Peng Wu (2021) An interactive detector for spatial associations, International Journal of Geographical Information Science, 35:8, 1676-1701, DOI:10.1080/13658816.2021.1882680

### Examples

```
## Not run:
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
coord = usfi |>
  st_centroid() |>
  st_coordinates()
wt = inverse_distance_weight(coord[,1], coord[,2])
usfi = st_drop_geometry(usfi)
cpsd_disc(SUHI ~ NDVI + BH, data = usfi, wt = wt, cores = 6)

## End(Not run)
```

### Description

Function for calculate compensated power of spatial determinant  $Q_s$ .

## Usage

```
cpsd_spade(yobs, xobs, xdisc, wt)
```

## Arguments

yobs	Variable Y
xobs	The original un-discretized covariable X.
xdisc	The discretized covariable X.
wt	The spatial weight matrix.

## Details

The power of compensated spatial determinant formula is  $Q_s = \frac{q_s}{q_{s \text{ in } forkep}} = \frac{1 - \frac{\sum_{h=1}^L N_h \Gamma_{kdep}}{N \Gamma_{totaldep}}}{1 - \frac{\sum_{h=1}^L N_h \Gamma_{hind}}{N \Gamma_{totalind}}}$

## Value

A value of compensated power of spatial determinant  $Q_s$ .

## Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

## References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

## Examples

```
## Not run:
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
coord = usfi |>
  st_centroid() |>
  st_coordinates()
wt = inverse_distance_weight(coord[,1], coord[,2])
BH = usfi$BH
BH_disc = st_unidisc(usfi$BH, 12)
SUHI = usfi$SUHI
cpsd_spade(SUHI, BH, BH_disc, wt)

## End(Not run)
```

`ecological_detector`    *ecological detector*

### Description

Compare the effects of two factors  $X_1$  and  $X_2$  on the spatial distribution of the attribute  $Y$ .

### Usage

```
ecological_detector(y, x1, x2, alpha = 0.95)
```

### Arguments

<code>y</code>	Dependent variable, continuous numeric vector.
<code>x1</code>	Covariate $X_1$ , factor, character or discrete numeric.
<code>x2</code>	Covariate $X_2$ , factor, character or discrete numeric.
<code>alpha</code>	(optional) Confidence level of the interval,default is 0.95.

### Value

A list contains F statistics, P-values, and is there a significant difference between the two factors  $X_1$  and  $X_2$  on the spatial distribution of the attribute  $Y$ .

### Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

### Examples

```
ecological_detector(y = 1:7,
                     x1 = c('x',rep('y',3),rep('z',3)),
                     x2 = c(rep('a',2),rep('b',2),rep('c',3)))
```

`factor_detector`    *factor detector*

### Description

The factor detector q-statistic measures the spatial stratified heterogeneity of a variable Y, or the determinant power of a covariate X of Y.

### Usage

```
factor_detector(y, x)
```

**Arguments**

- |   |  |
|---|--|
| y | Variable Y, continuous numeric vector.               |
| x | Covariable X, factor, character or discrete numeric. |

**Value**

A list contains the Q-statistic and the P-value.

**Author(s)**

Wenbo Lv <luyu.geosocial@gmail.com>

**Examples**

```
factor_detector(y = 1:7,x = c('x',rep('y',3),rep('z',3)))
```

F\_informationloss      *measure information loss by information entropy*

**Description**

Function for measure information loss by information entropy.

**Usage**

```
F_informationloss(xvar, xdisc)
```

**Arguments**

- |       |                                     |
|-------|-------------------------------------|
| xvar  | The original un-discretized vector. |
| xdisc | The discretized vector.             |

**Details**

The information loss measured by information entropy formula is 
$$F = - \sum_{i=1}^N p_{(i)} \log_2 p_{(i)} - \left( - \sum_{h=1}^L p_{(h)} \log_2 p_{(h)} \right)$$

**Value**

A numeric value of information loss measured by information entropy.

**Author(s)**

Wenbo Lv <luyu.geosocial@gmail.com>

## Examples

```
F_informationloss(1:7,c('x',rep('y',3),rep('z',3)))
```

gd	<i>original geographical detector model</i>
----	---

## Description

Function for original geographical detector model.

## Usage

```
gd(formula, data, type = "factor", ...)
```

## Arguments

formula	A formula of geographical detector model.
data	A data.frame or tibble of observation data.
type	(optional) The type of geographical detector, which must be one of <code>factor</code> (default), <code>interaction</code> , <code>risk</code> , <code>ecological</code> .
...	(optional) Specifies the size of the alpha (confidence level). Default is 0.95.

## Value

A tibble of the corresponding result is stored under the corresponding detector type.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Jin-Feng Wang, Xin-Hu Li, George Christakos, Yi-Lan Liao, Tin Zhang, XueGu & Xiao-Ying Zheng (2010) Geographical Detectors-Based Health Risk Assessment and its Application in the Neural Tube Defects Study of the Heshun Region, China, International Journal of Geographical Information Science, 24:1, 107-127, DOI: 10.1080/13658810802443457

## Examples

```
gd(y ~ x1 + x2,
  tibble::tibble(y = 1:7,
                x1 = c('x',rep('y',3),rep('z',3)),
                x2 = c(rep('a',2),rep('b',2),rep('c',3))))
```

  

```
gd(y ~ x1 + x2,
  tibble::tibble(y = 1:7,
```

```

x1 = c('x',rep('y',3),rep('z',3)),
x2 = c(rep('a',2),rep('b',2),rep('c',3))),
type = 'interaction')

gd(y ~ x1 + x2,
  tibble::tibble(y = 1:7,
                 x1 = c('x',rep('y',3),rep('z',3)),
                 x2 = c(rep('a',2),rep('b',2),rep('c',3))),
  type = 'risk',alpha = 0.95)

gd(y ~ x1 + x2,
  tibble::tibble(y = 1:7,
                 x1 = c('x',rep('y',3),rep('z',3)),
                 x2 = c(rep('a',2),rep('b',2),rep('c',3))),
  type = 'ecological',alpha = 0.95)

```

**gd\_bestunidisc***best univariate discretization based on geodetector q-statistic***Description**

Function for determining the best univariate discretization based on geodetector q-statistic.

**Usage**

```
gd_bestunidisc(
  formula,
  data,
  discnum = NULL,
  discmethod = NULL,
  cores = 1,
  return_disc = TRUE,
  seed = 123456789,
  ...
)
```

**Arguments**

<code>formula</code>	A formula of best univariate discretization.
<code>data</code>	A <code>data.frame</code> or <code>tibble</code> of observation data.
<code>discnum</code>	(optional) A vector of number of classes for discretization. Default is 3:22.
<code>discmethod</code>	(optional) A vector of methods for discretization,default is using <code>c("sd","equal","pretty","quantile", "gdi", "vadis")</code> .
<code>cores</code>	(optional) A positive integer(default is 1). If <code>cores &gt; 1</code> , a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.

<code>return_disc</code>	(optional) Whether or not return discretized result used the optimal parameter. Default is TRUE.
<code>seed</code>	(optional) Random seed number, default is 123456789. Setting random seed is useful when the sample size is greater than 3000(the default value for largeN) and the data is discretized by sampling 10%(the default value for samp_prop in <code>st_unidisc()</code> ).
<code>...</code>	(optional) Other arguments passed to <code>st_unidisc()</code> .

**Value**

A list with the optimal parameter in the provided parameter combination with `k`, `method` and `disc`(when `return_disc` is TRUE).

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

**Examples**

```
## Not run:
library(terra)
library(tidyverse)
fvcpath = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/",fvcpath))
fvc = terra::aggregate(fvc,fact = 5)
fvc = as_tibble(terra::as.data.frame(fvc,na.rm = T))
g = gd_bestunidisc(fvc ~ .,data = select(fvc,-lulc),discnum = 3:15,cores = 6)
g

## End(Not run)
```

`generate_subsets`      *generate subsets of a set*

**Description**

generate subsets of a set

**Usage**

```
generate_subsets(set, empty = TRUE, self = TRUE)
```

**Arguments**

<code>set</code>	A vector including the empty set and the set itself. Default is TRUE.
<code>empty</code>	(optional) When <code>empty</code> is TRUE, the generated subset includes the empty set, otherwise the empty set is removed. Default is TRUE.
<code>self</code>	(optional) When <code>self</code> is TRUE, the resulting subset includes the set itself, otherwise the set itself is removed. Default is TRUE.

**Value**

A list with the subsets

**Examples**

```
generate_subsets(letters[1:3])
generate_subsets(letters[1:3],empty = FALSE)
generate_subsets(letters[1:3],self = FALSE)
generate_subsets(letters[1:3],empty = FALSE,self = FALSE)
```

---

gozh*geographically optimal zones-based heterogeneity(GOZH) model*

---

**Description**

Function for geographically optimal zones-based heterogeneity(GOZH) model

**Usage**

```
gozh(formula, data, cores = 1, type = "factor", alpha = 0.95, ...)
```

**Arguments**

formula	A formula of GOZH model.
data	A data.frame or tibble of observation data.
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
type	(optional) The type of geographical detector,which must be factor(default), interaction, risk, ecological.You can run one or more types at one time.
alpha	(optional) Specifies the size of confidence level.Default is 0.95.
...	(optional) Other arguments passed to rpart_disc().

**Value**

A list of GOZH model result.

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Luo, P., Song, Y., Huang, X., Ma, H., Liu, J., Yao, Y., & Meng, L. (2022). Identifying determinants of spatio-temporal disparities in soil moisture of the Northern Hemisphere using a geographically optimal zones-based heterogeneity model. *ISPRS Journal of Photogrammetry and Remote Sensing: Official Publication of the International Society for Photogrammetry and Remote Sensing (ISPRS)*, 185, 111–128. <https://doi.org/10.1016/j.isprsjprs.2022.01.009>

## Examples

```
data('ndvi')
g = gozh(NDVIchange ~ ., data = ndvi)
g
```

gozh\_detector

*geographically optimal zones-based heterogeneity detector*

## Description

Function for geographically optimal zones-based heterogeneity detector.

## Usage

```
gozh_detector(formula, data, cores = 1, type = "factor", alpha = 0.95, ...)
```

## Arguments

formula	A formula of GOZH detector.
data	A data.frame or tibble of observation data.
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
type	(optional) The type of geographical detector,which must be one of factor(default), interaction, risk, ecological.
alpha	(optional) Confidence level of the interval,default is 0.95.
...	(optional) Other arguments passed to rpart_disc().

## Value

A list of the corresponding result is stored under the corresponding detector type.

## Note

Only one type of detector is supported in a gozh\_detector() run at a time.

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

**References**

Luo, P., Song, Y., Huang, X., Ma, H., Liu, J., Yao, Y., & Meng, L. (2022). Identifying determinants of spatio-temporal disparities in soil moisture of the Northern Hemisphere using a geographically optimal zones-based heterogeneity model. *ISPRS Journal of Photogrammetry and Remote Sensing: Official Publication of the International Society for Photogrammetry and Remote Sensing (ISPRS)*, 185, 111–128. <https://doi.org/10.1016/j.isprsjprs.2022.01.009>

**Examples**

```
data('ndvi')
g = gozh_detector(NDVIchange ~ ., data = ndvi)
g
```

---

idsa

*interactive detector for spatial associations(IDSA)*

---

**Description**

Function for interactive detector for spatial associations model.

**Usage**

```
idsa(
  formula,
  data,
  wt = NULL,
  overlaymethod = "and",
  locations = NULL,
  discnum = NULL,
  discmethod = NULL,
  strategy = 2L,
  increase_rate = 0.05,
  cores = 6,
  seed = 123456789,
  alpha = 0.95,
  ...
)
```

## Arguments

formula	A formula of IDSA model.
data	A data.frame or tibble of observation data.
wt	(optional) The spatial weight matrix. When wt is not provided, must provide locations. And gdverse will use locations columns to construct spatial weight use <code>inverse_distance_weight()</code> .
overlaymethod	(optional) Spatial overlay method. One of and, or, intersection. Default is and.
locations	(optional) The geospatial locations coordinate columns name which in data. Useful and must provided when wt is not provided. When wt is provided, locations is not need.
discnum	(optional) Number of multilevel discretization. Default will use 3:22.
discmethod	(optional) The discretization methods. Default all use quantile. More details to see <code>st_unidisc()</code> .
strategy	(optional) Discretization strategy. When strategy is 1L, choose the highest SPADE model q-statistics to determinate optimal spatial data discretization parameters. When strategy is 2L, The optimal discrete parameters of spatial data are selected by combining LOESS model.
increase_rate	(optional) The critical increase rate of the number of discretization. Default is 5%.
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
seed	(optional) Random number seed, default is 123456789.
alpha	(optional) Specifies the size of confidence level. Default is 0.95.
...	(optional) Other arguments passed to <code>cpsd_disc()</code> .

## Value

A list with PID values tibble under different spatial overlays and performance evaluation indicators.

## Note

The IDSA model requires at least  $2^n - 1$  calculations when has  $n$  explanatory variables. When there are more than 10 explanatory variables, carefully consider the computational burden of this model. When there are a large number of explanatory variables, the data dimensionality reduction method can be used to ensure the trade-off between analysis results and calculation speed.

## Author(s)

Wenbo Lv <[llyu.geosocial@gmail.com](mailto:llyu.geosocial@gmail.com)>

## References

Yongze Song & Peng Wu (2021) An interactive detector for spatial associations, International Journal of Geographical Information Science, 35:8, 1676-1701, DOI:10.1080/13658816.2021.1882680

## Examples

```
## Not run:
data('sim')
g = idsa(y ~ ., data = sim, locations = c('lo','la'),
          discvar = c("xa","xb","xc"), cores = 6)
g

## End(Not run)
```

interaction\_detector *interaction detector*

## Description

Identify the interaction between different risk factors, that is, assess whether factors  $X_1$  and  $X_2$  together increase or decrease the explanatory power of the dependent variable  $Y$ , or whether the effects of these factors on  $Y$  are independent of each other.

## Usage

```
interaction_detector(y, x1, x2)
```

## Arguments

<code>y</code>	Dependent variable, continuous numeric vector.
<code>x1</code>	Covariable $X_1$ , factor, character or discrete numeric.
<code>x2</code>	Covariable $X_2$ , factor, character or discrete numeric.

## Value

A list contains the Q statistic when the factors  $X_1$  and  $X_2$  act on  $Y$  alone and the Q statistic when the two interact on  $Y$  together with the result type of the interaction detector.

## Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

## Examples

```
interaction_detector(y = 1:7,
                     x1 = c('x',rep('y',3),rep('z',3)),
                     x2 = c(rep('a',2),rep('b',2),rep('c',3)))
```

---

**inverse\_distance\_weight**  
*calculate inverse distance weight*

---

## Description

Function for calculate inverse distance weight.

## Usage

```
inverse_distance_weight(locx, locy, power = 1, is_arc = FALSE)
```

## Arguments

locx	The x axis location.
locy	The y axis location.
power	(optional) Default is 1. Set to 2 for gravity weights.
is_arc	(optional) FALSE (default) or TRUE, whether to compute arc distance.

## Details

The inverse distance weight formula is  $w_{ij} = 1/d_{ij}^\alpha$

## Value

A inverse distance weight matrices with class of `matrix`.

## Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

## Examples

```
x = 1:10
y = 1:10
inverse_distance_weight(x,y)
inverse_distance_weight(x,y,is_arc = TRUE)
```

---

lesh	<i>locally explained heterogeneity(LESH) model</i>
------	--

---

## Description

Function for locally explained heterogeneity model.

## Usage

```
lesh(formula, data, cores = 1, ...)
```

## Arguments

formula	A formula of LESH model.
data	A data.frame or tibble of observation data.
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
...	(optional) Other arguments passed to rpart_disc().

## Value

A list of LESH model result.

## Note

The LESH model requires at least  $2^n - 1$  calculations when has  $n$  explanatory variables. When there are more than 10 explanatory variables, carefully consider the computational burden of this model. When there are a large number of explanatory variables, the data dimensionality reduction method can be used to ensure the trade-off between analysis results and calculation speed.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Li, Y., Luo, P., Song, Y., Zhang, L., Qu, Y., & Hou, Z. (2023). A locally explained heterogeneity model for examining wetland disparity. International Journal of Digital Earth, 16(2), 4533–4552. <https://doi.org/10.1080/17538947.2023.2271883>

## Examples

```
## Not run:
data('ndvi')
g = lesh(NDVIchange ~ ., data = ndvi, cores = 6)
g

## End(Not run)
```

**loess\_optdiscnum**      *determine optimal spatial data discretization for individual variables*

## Description

Function for determining optimal spatial data discretization for individual variables based on locally estimated scatterplot smoothing (LOESS) model.

## Usage

```
loess_optdiscnum(qvec, discnumvec, increase_rate = 0.05)
```

## Arguments

qvec	A numeric vector of q statistics.
discnumvec	A numeric vector of break numbers corresponding to qvec.
increase_rate	(optional) The critical increase rate of the number of discretization. Default is 5%.

## Value

A optimal number of spatial data discretization.

## Note

When `increase_rate` is not satisfied by the calculation, `increase_rate*0.1` is used first. At this time, if `increase_rate*0.1` is not satisfied again, the discrete number corresponding to the highest Q-statistic is selected as a return.

Note that `gVERSE` sorts `discnumvec` from smallest to largest and keeps `qvec` in one-to-one correspondence with `discnumvec`.

## Author(s)

Wenbo Lv <[llyu.geosocial@gmail.com](mailto:llyu.geosocial@gmail.com)>

## References

Yongze Song & Peng Wu (2021) An interactive detector for spatial associations, International Journal of Geographical Information Science, 35:8, 1676-1701, DOI:10.1080/13658816.2021.1882680

## Examples

```
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
3:10 %>%
  purrr::map_dbl(\(.k) st_unidisc(usfi$NDVI, .k) %>%
    factor_detector(usfi$SUHI, .) %>%
    {.[[1]]}) %>%
  loess_optdiscnum(3:10)
```

**loess\_optscale**      *determine optimal spatial data analysis scale*

## Description

Function for determining optimal spatial data analysis scale based on locally estimated scatter plot smoothing (LOESS) model.

## Usage

```
loess_optscale(qvec, spscalevec, increase_rate = 0.05)
```

## Arguments

<code>qvec</code>	A numeric vector of q statistics.
<code>spscalevec</code>	A numeric vector of spatial scales corresponding to <code>qvec</code> .
<code>increase_rate</code>	(optional) The critical increase rate of the number of discretization. Default is 5%.

## Value

A optimal number of spatial scale

## Author(s)

Wenbo Lv <[llyu.geosocial@gmail.com](mailto:llyu.geosocial@gmail.com)>

## Examples

```
## Not run:
library(tidyverse)
fvcpath = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/", fvcpath))
fvc1000 = fvc %>%
  terra::as.data.frame(na.rm = T) %>%
  as_tibble()
fvc5000 = fvc %>%
```

```

terra::aggregate(fact = 5) %>%
terra::as.data.frame(na.rm = T) %>%
as_tibble()
qv1000 = factor_detector(fvc1000$fvc,
                         st_unidisc(fvc1000$premax,10,'quantile'))[[1]]
qv5000 = factor_detector(fvc5000$fvc,
                         st_unidisc(fvc5000$premax,10,'quantile'))[[1]]
loess_optscale(c(qv1000,qv5000),c(1000,5000))

## End(Not run)

```

ndvi

*dataset of NDVI changes and its influencing factors***Description**

dataset of NDVI changes and its influencing factors, modified from GD package.

**Usage**

ndvi

**Format**

ndvi: A tibble with 713 rows and 7 variables

NTDs

*NTDs data***Description**

The data were obtained by preprocessing use sf and tidyverse.

**Usage**

NTDs

**Format**

NTDs: A tibble with 185 rows and 4 variable columns and 2 location columns, modified from geodetector package.

---

`opgd`*optimal parameters-based geographical detector(OPGD) model*

---

## Description

Function for optimal parameters-based geographical detector(OPGD) model.

## Usage

```
opgd(  
  formula,  
  data,  
  discvar,  
  discnum = NULL,  
  discmethod = NULL,  
  cores = 1,  
  type = "factor",  
  alpha = 0.95,  
  ...  
)
```

## Arguments

formula	A formula of OPGD model.
data	A data.frame or tibble of observation data.
discvar	Name of continuous variable columns that need to be discretized. Noted that when formula has discvar, data must have these columns.
discnum	(optional) A vector of number of classes for discretization. Default is 3:22.
discmethod	(optional) A vector of methods for discretization, default is using c("sd", "equal", "pretty", "quantile", "gdi", "gdiplus").
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package will be used to cluster with that many cores is created and used. You can also supply a cluster object.
type	(optional) The type of geographical detector, which must be factor(default), interaction, risk, ecological. You can run one or more types at one time.
alpha	(optional) Specifies the size of confidence level. Default is 0.95.
...	(optional) Other arguments passed to gd_bestunidisc(). A useful parameter is seed, which is used to set the random number seed.

## Value

A list of the OPGD model result.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Song, Y., Wang, J., Ge, Y. & Xu, C. (2020) An optimal parameters-based geographical detector model enhances geographic characteristics of explanatory variables for spatial heterogeneity analysis: Cases with different types of spatial data, *GIScience & Remote Sensing*, 57(5), 593-610. doi: 10.1080/15481603.2020.1760434.

## Examples

```
## Not run:
library(terra)
library(tidyverse)
fvcpath = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/", fvcpath))
fvc = terra::aggregate(fvc, fact = 5)
fvc = as_tibble(terra::as.data.frame(fvc, na.rm = T))
opgd(fvc ~ ., data = fvc,
discvar = names(select(fvc,-c(fvc,lulc))),
cores = 6, type =c('factor','interaction'))

## End(Not run)
```

**pid\_idsa**

*IDSA Q-saistics PID*

## Description

IDSA Q-saistics PID

## Usage

```
pid_idsa(formula, rawdata, discdata, wt, overlaymethod = "and")
```

## Arguments

<b>formula</b>	A formula for IDSA Q-saistics
<b>rawdata</b>	Raw observation data
<b>discdata</b>	Discrete explanatory variables data
<b>wt</b>	Spatial weight matrix
<b>overlaymethod</b>	(optional) Spatial overlay method. One of <b>and</b> , <b>or</b> , <b>intersection</b> . Default is <b>and</b> .

## Details

$$Q_{IDSA} = \frac{\theta_r}{\phi}$$

## Value

The value of IDSA Q-saistics PID.

## Examples

```
## Not run:  
library(sf)  
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>  
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "WAR", "SUHI")))  
coord = usfi |>  
  st_centroid() |>  
  st_coordinates()  
wt = inverse_distance_weight(coord[,1], coord[,2])  
usf = usfi |>  
  st_drop_geometry() |>  
  dplyr::mutate(dplyr::across(1:3, \(.x) st_unidisc(.x, 12)))  
pid_idsa('NDVI~.', rawdata = usfi, disccdata = usf, wt = wt)  
  
## End(Not run)
```

---

plot.ecological\_detector  
*plot ecological detector*

---

## Description

S3 method to plot output for ecological detector in gd().

## Usage

```
## S3 method for class 'ecological_detector'  
plot(x, ...)
```

## Arguments

x               Return by gd().  
...              (optional) Other arguments passed to ggplot2::theme().

## Value

A ggplot2 layer

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

`plot.factor_detector` *plot factor detector result*

### Description

S3 method to plot output for factor detector in `gd()`.

### Usage

```
## S3 method for class 'factor_detector'
plot(x, slicenum = 2, alpha = 0.95, ...)
```

### Arguments

<code>x</code>	Return by <code>gd()</code> .
<code>slicenum</code>	(optional) The number of labels facing inward. Default is 2.
<code>alpha</code>	(optional) Confidence level. Default is 0.95.
<code>...</code>	(optional) Other arguments passed to <code>ggplot2::theme()</code> .

### Value

A `ggplot2` layer.

### Author(s)

Wenbo Lv <[lvyu.geosocial@gmail.com](mailto:lvyu.geosocial@gmail.com)>

`plot.idsa_result` *plot IDSA risk result*

### Description

S3 method to plot output for IDSA risk result in `idsa()`.

### Usage

```
## S3 method for class 'idsa_result'
plot(x, ...)
```

### Arguments

<code>x</code>	Return by <code>idsa()</code> .
<code>...</code>	(optional) Other arguments passed to <code>ggplot2::theme()</code> .

**Value**

A ggplot2 layer

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

---

```
plot.interaction_detector  
    plot interaction detector result
```

---

**Description**

S3 method to plot output for interaction detector in gd().

**Usage**

```
## S3 method for class 'interaction_detector'  
plot(x, alpha = 1, ...)
```

**Arguments**

x	Return by gd().
alpha	(optional) Picture transparency. Default is 1.
...	(optional) Other arguments passed to ggplot2::theme().

**Value**

A ggplot2 layer

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

`plot.lesh_result`      *plot LESH model result*

## Description

S3 method to plot output for LESH model interaction result in `lesh()`.

## Usage

```
## S3 method for class 'lesh_result'
plot(x, pie = TRUE, scatter = FALSE, ..., scatter_alpha = 1)
```

## Arguments

<code>x</code>	<code>x</code> Return by <code>lesh()</code> .
<code>pie</code>	(optional) Whether to draw the interaction contributions. Default is TRUE.
<code>scatter</code>	(optional) Whether to draw the interaction direction diagram. Default is FALSE.
<code>...</code>	(optional) Other arguments passed to <code>ggplot2::theme()</code> .
<code>scatter_alpha</code>	(optional) Picture transparency. Default is 1.

## Details

When both `scatter` and `pie` are set to TRUE in RStudio, enlarge the drawing frame for normal display.

## Value

A `ggplot2` layer.

## Author(s)

Wenbo Lv <[lvyu.geosocial@gmail.com](mailto:lvyu.geosocial@gmail.com)>

## Examples

```
## Not run:
data('ndvi')
g = lesh(NDVIchange ~ ., data = ndvi, cores = 6)
plot(g)

## End(Not run)
```

---

```
plot.risk_detector      plot risk detector
```

---

**Description**

S3 method to plot output for risk detector in gd().

**Usage**

```
## S3 method for class 'risk_detector'  
plot(x, ...)
```

**Arguments**

x                   Return by gd().  
...                  (optional) Other arguments passed to ggplot2::theme().

**Value**

A ggplot2 layer

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

---

```
plot.sesu_gozh      plot gozh sesu
```

---

**Description**

S3 method to plot output for gozh sesu in sesu\_gozh().

**Usage**

```
## S3 method for class 'sesu_gozh'  
plot(x, ...)
```

**Arguments**

x                   Return by sesu\_gozh().  
...                  (optional) Other arguments passed to ggplot2::theme().

**Value**

A ggplot2 layer.

**Author(s)**

Wenbo Lv <lvyu.geosocial@gmail.com>

**plot.sesu\_opgd**      *plot opgd sesu*

**Description**

S3 method to plot output for opgd sesu in `sesu_opgd()`.

**Usage**

```
## S3 method for class 'sesu_opgd'
plot(x, ...)
```

**Arguments**

<code>x</code>	Return by <code>sesu_opgd()</code> .
<code>...</code>	(optional) Other arguments passed to <code>ggplot2::theme()</code> .

**Value**

A `ggplot2` layer.

**Author(s)**

Wenbo Lv <lvyu.geosocial@gmail.com>

**plot.spade\_result**      *plot SPADE power of spatial and multilevel discretization determinant*

**Description**

S3 method to plot output for SPADE power of spatial and multilevel discretization determinant from `spade()`.

**Usage**

```
## S3 method for class 'spade_result'
plot(x, slicenum = 2, alpha = 0.95, ...)
```

**Arguments**

- |          |  |
|----------|--|
| x        | Return by spade().The number of labels facing inward.        |
| slicenum | (optional) The number of labels facing inward. Default is 2. |
| alpha    | (optional) Confidence level.Default is 0.95.                 |
| ...      | (optional) Other arguments passed to ggplot2::theme().       |

**Value**

A ggplot2 layer.

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

---

**print.ecological\_detector**  
*print ecological\_detector*

---

**Description**

S3 method to format output for ecological detector in gd().

**Usage**

```
## S3 method for class 'ecological_detector'  
print(x, ...)
```

**Arguments**

- |     |  |
|-----|--|
| x   | Return by gd().                                      |
| ... | (optional) Other arguments passed to knitr::kable(). |

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

`print.factor_detector` *print factor detector*

### Description

S3 method to format output for factor detector in gd().

### Usage

```
## S3 method for class 'factor_detector'
print(x, ...)
```

### Arguments

<code>x</code>	Return by gd().
<code>...</code>	(optional) Other arguments passed to knitr::kable().

### Value

Formatted string output

### Author(s)

Wenbo Lv <lvy.geosocial@gmail.com>

`print.idsa_result` *print IDSA result*

### Description

S3 method to format output for IDSA model from idsa().

### Usage

```
## S3 method for class 'idsa_result'
print(x, ...)
```

### Arguments

<code>x</code>	Return by idsa().
<code>...</code>	(optional) Other arguments passed to knitr::kable().

### Value

Formatted string output

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

---

```
print.interaction_detector  
      print interaction detector
```

---

**Description**

S3 method to format output for interaction detector in gd().

**Usage**

```
## S3 method for class 'interaction_detector'  
print(x, ...)
```

**Arguments**

x	Return by gd().
...	(optional) Other arguments passed to knitr::kable().

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

---

```
print.lesh_result      print LESH model interaction result
```

---

**Description**

S3 method to format output for LESH model interaction result in lesh().

**Usage**

```
## S3 method for class 'lesh_result'  
print(x, ...)
```

**Arguments**

x	Return by lesh().
...	(optional) Other arguments passed to knitr::kable().

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

---

`print.rid_result`      *print RID result*

---

**Description**

S3 method to format output for RID model from `rid()`.

**Usage**

```
## S3 method for class 'rid_result'  
print(x, ...)
```

**Arguments**

`x`                  Return by `rid()`.  
`...`                (optional) Other arguments passed to `knitr::kable()`.

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

---

`print.risk_detector`      *print risk detector*

---

**Description**

S3 method to format output for risk detector in `gd()`.

**Usage**

```
## S3 method for class 'risk_detector'  
print(x, ...)
```

**Arguments**

- x Return by `gd()`.
- ... (optional) Other arguments passed to `knitr::kable()`.

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

---

`print.sesu_gozh`      *print gozh sesu*

---

**Description**

S3 method to format output for gozh sesu from `sesu_gozh()`.

**Usage**

```
## S3 method for class 'sesu_gozh'  
print(x, ...)
```

**Arguments**

- x Return by `sesu_gozh()`.
- ... (optional) Other arguments passed to `knitr::kable()`.

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

`print.sesu_opgd`      *print opgd sesu*

### Description

S3 method to format output for opgd sesu from `sesu_opgd()`.

### Usage

```
## S3 method for class 'sesu_opgd'
print(x, ...)
```

### Arguments

<code>x</code>	Return by <code>sesu_opgd()</code> .
...	(optional) Other arguments passed to <code>knitr::kable()</code> .

### Value

Formatted string output

### Author(s)

Wenbo Lv <[lvyu.geosocial@gmail.com](mailto:lvyu.geosocial@gmail.com)>

`print.spade_result`      *print SPADE power of spatial and multilevel discretization determinant*

### Description

S3 method to format output for SPADE power of spatial and multilevel discretization determinant from `spade()`.

### Usage

```
## S3 method for class 'spade_result'
print(x, ...)
```

### Arguments

<code>x</code>	Return by <code>spade()</code> .
...	Other arguments.

**Value**

Formatted string output

**Author(s)**

Wenbo Lv <luyu.geosocial@gmail.com>

psd\_iev

*PSD of an interaction of explanatory variables (PSD-IEV)*

**Description**

PSD of an interaction of explanatory variables (PSD-IEV)

**Usage**

```
psd_iev(discreddata, spzone, wt)
```

**Arguments**

discreddata	Discreted explanatory variables data. A tibble or dataframe .
spzone	Fuzzy overlay spatial zones. Returned from <code>st_fuzzyoverlay()</code> .
wt	Spatial weight matrix

**Details**

$$\phi = 1 - \frac{\sum_{i=1}^m \sum_{k=1}^{n_i} N_{i,k} \tau_{i,k}}{\sum_{i=1}^m N_i \tau_i}$$

**Value**

The Value of PSD-IEV

**Author(s)**

Wenbo Lv <luyu.geosocial@gmail.com>

**References**

Yongze Song & Peng Wu (2021) An interactive detector for spatial associations, International Journal of Geographical Information Science, 35:8, 1676-1701, DOI:10.1080/13658816.2021.1882680

**Examples**

```
data('NTDs')
wt = inverse_distance_weight(NTDs$X, NTDs$Y, power = 2)
sz = st_fuzzyoverlay(incidence ~ watershed + elevation + soilttype,
                     data = NTDs)
psd_iev(dplyr::select(NTDs,-c(X,Y,incidence)),sz,wt)
```

---

<code>psd_pseudop</code>	<i>calculate power of spatial determinant(PSD) and the corresponding pseudo-p value</i>
--------------------------	---

---

## Description

Function for calculate power of spatial determinant  $q_s$ .

## Usage

```
psd_pseudop(y, x, wt, cores = 6, seed = 123456789, permutations = 0)
```

## Arguments

<code>y</code>	Variable Y, continuous numeric vector.
<code>x</code>	Covariable X, factor, character or discrete numeric.
<code>wt</code>	The spatial weight matrix.
<code>cores</code>	(optional) A positive integer(default is 6). If cores > 1, use parallel computation.
<code>seed</code>	(optional) Random seed number, default is 123456789.
<code>permutations</code>	(optional) The number of permutations for the PSD computation. Default is 0, which means no pseudo-p values are calculated.

## Details

The power of spatial determinant formula is  $q_s = 1 - \frac{\sum_{h=1}^L N_h \Gamma_h}{N \Gamma}$

## Value

A tibble of power of spatial determinant and the corresponding pseudo-p value.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

## Examples

```
## Not run:
data('NTDs')
wt = inverse_distance_weight(NTDs$X, NTDs$Y, power = 2)
tictoc::tic()
pp = psd_pseudop(NTDs$incidence, NTDs$soiltype, wt)
tictoc::toc()
```

```
pp
## End(Not run)
```

psd\_spade

*power of spatial determinant(PSD)***Description**

Function for calculate power of spatial determinant  $q_s$ .

**Usage**

```
psd_spade(y, x, wt)
```

**Arguments**

- |    |  |
|----|--|
| y  | Variable Y, continuous numeric vector.               |
| x  | Covariable X, factor, character or discrete numeric. |
| wt | The spatial weight matrix.                           |

**Details**

The power of spatial determinant formula is  $q_s = 1 - \frac{\sum_{h=1}^L N_h \Gamma_h}{N \Gamma}$

**Value**

A value of power of spatial determinant  $q_s$ .

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

**References**

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

**Examples**

```
data('NTDs')
wt = inverse_distance_weight(NTDs$X, NTDs$Y, power = 2)
psd_spade(NTDs$incidence, NTDs$soiltype, wt)
```

---

<code>psmd_pseudop</code>	<i>power of spatial and multilevel discretization determinant(PSMD) and the corresponding pseudo-p value</i>
---------------------------	--

---

## Description

Function for calculate power of spatial and multilevel discretization determinant and the corresponding pseudo-p value.

## Usage

```
psmd_pseudop(
  formula,
  data,
  wt = NULL,
  locations = NULL,
  discnum = NULL,
  discmethod = NULL,
  cores = 6,
  seed = 123456789,
  permutations = 0,
  ...
)
```

## Arguments

<code>formula</code>	A formula of calculate power of spatial and multilevel discretization determinant $PSMDQ_s$ .
<code>data</code>	A data.frame or tibble of observation data.
<code>wt</code>	(optional) The spatial weight matrix. When <code>wt</code> is not provided, must provide <code>locations</code> . And gdverse will use <code>locations</code> columns to construct spatial weight use <code>inverse_distance_weight()</code> .
<code>locations</code>	(optional) The geospatial locations coordinate columns name which in <code>data</code> . Useful and must provided when <code>wt</code> is not provided.
<code>discnum</code>	(optional) Number of multilevel discretization. Default will use 3:22.
<code>discmethod</code>	(optional) The discretization methods. Default will use <code>quantile</code> . When <code>discmethod</code> is robust use <code>robust_disc()</code> , others use <code>st_unidisc()</code> . Now only support one <code>discmethod</code> at one time.
<code>cores</code>	(optional) A positive integer(default is 6). If <code>cores &gt; 1</code> , use parallel computation.
<code>seed</code>	(optional) Random seed number, default is 123456789.
<code>permutations</code>	(optional) The number of permutations for the PSD computation. Default is 0, which means no pseudo-p values are calculated.
<code>...</code>	(optional) Other arguments passed to <code>st_unidisc()</code> or <code>robust_disc()</code> .

## Details

The power of spatial and multilevel discretization determinant formula is  $PSMDQ_s = MEAN(Q_s)$

## Value

A tibble of power of spatial and multilevel discretization determinant and the corresponding pseudo-p value.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

## Examples

```
## Not run:
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
coord = usfi |>
  st_centroid() |>
  st_coordinates()
usfi = usfi |>
  dplyr::bind_cols(coord) |>
  st_drop_geometry()
tictoc::tic()
pp = psmd_pseudop('SUHI ~ BH', data = dplyr::select(usfi, SUHI, BH, X, Y),
                  locations = c('X', 'Y'), cores = 6)
tictoc::toc()
pp

## End(Not run)
```

## Description

Function for calculate power of spatial and multilevel discretization determinant  $PSMDQ_s$ .

## Usage

```
psmd_spade(
  formula,
  data,
  wt = NULL,
  locations = NULL,
  discnum = NULL,
  discmethod = NULL,
  cores = 1,
  seed = 123456789,
  ...
)
```

## Arguments

<code>formula</code>	A formula of calculate power of spatial and multilevel discretization determinant $PSMDQ_s$ .
<code>data</code>	A data.frame or tibble of observation data.
<code>wt</code>	(optional) The spatial weight matrix. When <code>wt</code> is not provided, must provide <code>locations</code> . And gdverse will use <code>locations</code> columns to construct spatial weight use <code>inverse_distance_weight()</code> .
<code>locations</code>	(optional) The geospatial locations coordinate columns name which in <code>data</code> . Useful and must provided when <code>wt</code> is not provided.
<code>discnum</code>	(optional) Number of multilevel discretization. Default will use 3:22.
<code>discmethod</code>	(optional) The discretization methods. Default will use <code>quantile</code> . When <code>discmethod</code> is robust use <code>robust_disc()</code> , others use <code>st_unidisc()</code> . Now only support one <code>discmethod</code> at one time.
<code>cores</code>	(optional) A positive integer(default is 1). If <code>cores &gt; 1</code> , use parallel computation.
<code>seed</code>	(optional) Random seed number, default is 123456789.
<code>...</code>	(optional) Other arguments passed to <code>st_unidisc()</code> or <code>robust_disc()</code> .

## Details

The power of spatial and multilevel discretization determinant formula is  $PSMDQ_s = MEAN(Q_s)$

## Value

A value of power of spatial and multilevel discretization determinant  $PSMDQ_s$ .

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

## Examples

```
## Not run:
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
coord = usfi |>
  st_centroid() |>
  st_coordinates()
usfi = usfi |>
  dplyr::bind_cols(coord) |>
  st_drop_geometry()
psmd_spade('SUHI ~ BH', data = dplyr::select(usfi, SUHI, BH, X, Y),
           locations = c('X', 'Y'), cores = 6)

## End(Not run)
```

## rescale\_vector

*rescale continuous vector to specified minimum and maximum*

## Description

rescale continuous vector to specified minimum and maximum

## Usage

```
rescale_vector(x, to_left = 0, to_right = 1)
```

## Arguments

x	A continuous numeric vector.
to_left	(optional) Specified minimum. Default is 0.
to_right	(optional) Specified maximum. Default is 1.

## Value

A continuous vector which has rescaled.

## Examples

```
rescale_vector(c(-5,1,5),0.01,0.99)
```

---

rgd	<i>robust geographical detector(RGD) model</i>
-----	--

---

## Description

Function for robust geographical detector(RGD) model.

## Usage

```
rgd(
  formula,
  data,
  discvar,
  discnum = NULL,
  minsize = NULL,
  cores = 1,
  type = "factor",
  alpha = 0.95
)
```

## Arguments

formula	A formula of RGD model.
data	A data.frame or tibble of observation data.
discvar	Name of continuous variable columns that need to be discretized. Noted that when formula has discvar, data must have these columns.
discnum	A numeric vector of discretized classes of columns that need to be discretized. Default all discvar use 10.
minsize	(optional) The min size of each discretization group. Default all use 1.
cores	(optional) Positive integer(default is 1). If cores > 1, use python's joblib package to parallel computation.
type	(optional) The type of geographical detector, which must be factor(default), interaction, risk, ecological. You can run one or more types at one time.
alpha	(optional) Specifies the size of confidence level. Default is 0.95.

## Value

A list of the RGD model result.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Zhang, Z., Song, Y.\*, & Wu, P., 2022. Robust geographical detector. International Journal of Applied Earth Observation and Geoinformation. 109, 102782. DOI: 10.1016/j.jag.2022.102782.

## Examples

```
## Not run:
data('ndvi')
reticulate::use_condaenv('geocompy')
g = rgd(NDVIchange ~ ., data = ndvi, dicsvar = names(ndvi)[-1],
cores = 6, type =c('factor','interaction'))

## End(Not run)
```

rid	<i>robust interaction detector(RID) model</i>
-----	---

## Description

Function for robust interaction detector(RID) model.

## Usage

```
rid(
  formula,
  data,
  overlaymethod = "and",
  discvar,
  discnum = NULL,
  minsize = NULL,
  cores = 1
)
```

## Arguments

formula	A formula of RID model.
data	A data.frame or tibble of observation data.
overlaymethod	(optional) Spatial overlay method. One of and, or, intersection. Default is and.
discvar	Name of continuous variable columns that need to be discretized. Noted that when formula has discvar, data must have these columns.
discnum	A numeric vector of discretized classes of columns that need to be discretized. Default all discvar use 10.
minsize	(optional) The min size of each discretization group. Default all use 1.
cores	(optional) Positive integer(default is 1). If cores > 1, use parallel computation.

## Value

A list of the RID model result.

## Note

For bivariate spatial interactions, use the RGD function and specify the type parameter as interaction.

The RID model requires at least  $2^n - 1$  calculations when has  $n$  explanatory variables. When there are more than 10 explanatory variables, carefully consider the computational burden of this model. When there are a large number of explanatory variables, the data dimensionality reduction method can be used to ensure the trade-off between analysis results and calculation speed.

## Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

## References

Zhang, Z., Song, Y., Karunaratne, L., & Wu, P. (2024). Robust interaction detector: A case of road life expectancy analysis. *Spatial Statistics*, 59(100814), 100814. <https://doi.org/10.1016/j.spasta.2024.100814>

## Examples

```
## Not run:
data('sim')
reticulate::use_condaenv('geocompy')
g = rid(y ~ ., data = sim %>% dplyr::select(-dplyr::any_of(c('lo','la'))),
         discvar = c("xa","xb","xc"), discnum = 4, cores = 6)
g

## End(Not run)
```

*risk\_detector*

*risk\_detector*

## Description

Determine whether there is a significant difference between the attribute means of two subregions.

## Usage

```
risk_detector(y, x, alpha = 0.95)
```

## Arguments

y	Variable Y, continuous numeric vector.
x	Covariable X, factor, character or discrete numeric.
alpha	(optional) Confidence level of the interval,default is 0.95.

## Value

A tibble contains different combinations of covariate X level and student t-test statistics, degrees of freedom, p-values, and whether has risk (Yes or No).

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

**Examples**

```
risk_detector(y = 1:7,
               x = c('x', rep('y', 3), rep('z', 3)))
```

**robust\_disc**

*univariate discretization based on offline change point detection*

**Description**

Determines discretization interval breaks using an optimization algorithm for variance-based change point detection.

**Usage**

```
robust_disc(formula, data, discnum, minsize = NULL, cores = 1)
```

**Arguments**

formula	A formula of univariate discretization.
data	A data.frame or tibble of observation data.
discnum	A numeric vector of discretized classes of columns that need to be discretized.
minsize	(optional) The min size of each discretization group. Default all use 1.
cores	(optional) A positive integer(default is 1). If cores > 1, use python's joblib package to parallel computation.

**Value**

A tibble of discretized classes of columns which need to be discretized.

**Author(s)**

Wenbo Lv <llyu.geosocial@gmail.com>

**Examples**

```
## Not run:
library(terra)
library(tidyverse)
fvcpth = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/", fvcpth))
fvc = terra::aggregate(fvc, fact = 5)
fvc = as_tibble(terra::as.data.frame(fvc, na.rm = T))
```

```
new.fvc = robust_disc(fvc ~ ., data = select(fvc, -lulc), discnum = 10, cores = 6)
new.fvc

## End(Not run)
```

**rpart\_disc***discretization of variables based on recursive partitioning***Description**

discretization of variables based on recursive partitioning

**Usage**

```
rpart_disc(formula, data, ...)
```

**Arguments**

<code>formula</code>	A formula.
<code>data</code>	A data.frame or tibble of observation data.
<code>...</code>	(optional) Other arguments passed to <code>rpart::rpart()</code> .

**Value**

A vector that being discretized.

**Author(s)**

Wenbo Lv <lvy.geosocial@gmail.com>

**References**

Luo, P., Song, Y., Huang, X., Ma, H., Liu, J., Yao, Y., & Meng, L. (2022). Identifying determinants of spatio-temporal disparities in soil moisture of the Northern Hemisphere using a geographically optimal zones-based heterogeneity model. *ISPRS Journal of Photogrammetry and Remote Sensing: Official Publication of the International Society for Photogrammetry and Remote Sensing (ISPRS)*, 185, 111–128. <https://doi.org/10.1016/j.isprsjprs.2022.01.009>

**Examples**

```
## Not run:
data('ndvi')
rpart_disc(NDVIchange ~ ., data = ndvi)

## End(Not run)
```

---

sesu\_gozh*comparison of size effects of spatial units based on GOZH*

---

## Description

Function for comparison of size effects of spatial units in spatial heterogeneity analysis based on geographically optimal zones-based heterogeneity(GOZH) model.

## Usage

```
sesu_gozh(
  formula,
  datalist,
  su,
  cores = 1,
  strategy = 2L,
  increase_rate = 0.05,
  alpha = 0.95,
  ...
)
```

## Arguments

formula	A formula of comparison of size effects of spatial units.
datalist	A list of <code>data.frame</code> or <code>tibble</code> .
su	A vector of sizes of spatial units.
cores	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
strategy	(optional) Calculation strategies of Q statistics at different scales. Default is 2L, see details for more contents.
increase_rate	(optional) The critical increase rate of the number of discretization. Default is 5%.
alpha	(optional) Specifies the size of confidence level. Default is 0.95.
...	(optional) Other arguments passed to <code>rpart_disc()</code> .

## Details

When `strategy` is 1, use the same process as `sesu_opgd()`.If not, all explanatory variables are used to generate a unique Q statistic corresponding to the data in the `datalist` based on `rpart_disc()` and `gd()`, and then `loess_optscale()`is used to determine the optimal analysis scale.

## Value

A list with `sesu`(size effects of spatial units),`optsu`(optimal spatial unit) and `strategy`(A number that represents the optimal analytical scale selection strategy).

### Author(s)

Wenbo Lv <lyu.geosocial@gmail.com>

### References

- Song, Y., Wang, J., Ge, Y. & Xu, C. (2020) An optimal parameters-based geographical detector model enhances geographic characteristics of explanatory variables for spatial heterogeneity analysis: Cases with different types of spatial data, *GIScience & Remote Sensing*, 57(5), 593-610. doi: 10.1080/15481603.2020.1760434.
- Luo, P., Song, Y., Huang, X., Ma, H., Liu, J., Yao, Y., & Meng, L. (2022). Identifying determinants of spatio-temporal disparities in soil moisture of the Northern Hemisphere using a geographically optimal zones-based heterogeneity model. *ISPRS Journal of Photogrammetry and Remote Sensing: Official Publication of the International Society for Photogrammetry and Remote Sensing (ISPRS)*, 185, 111–128. <https://doi.org/10.1016/j.isprsjprs.2022.01.009>

### Examples

```
## Not run:
library(tidyverse)
fvcpth = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/", fvcpth))
fvc1000 = fvc %>%
  terra::as.data.frame(na.rm = T) %>%
  as_tibble()
fvc5000 = fvc %>%
  terra::aggregate(fact = 5) %>%
  terra::as.data.frame(na.rm = T) %>%
  as_tibble()
sesu_gozh(fvc ~ .,
           datalist = list(fvc1000, fvc5000),
           su = c(1000,5000),
           cores = 6)

## End(Not run)
```

sesu\_opgd

*comparison of size effects of spatial units based on OPGD*

### Description

Function for comparison of size effects of spatial units in spatial heterogeneity analysis based on optimal parameters geographical detector(OPGD) model.

### Usage

```
sesu_opgd(
  formula,
  datalist,
```

```

    su,
    discvar,
    discnum = NULL,
    discmethod = NULL,
    cores = 1,
    increase_rate = 0.05,
    alpha = 0.95,
    ...
)

```

## Arguments

formula	A formula of comparison of size effects of spatial units.
datalist	A list of <code>data.frame</code> or <code>tibble</code> .
su	A vector of sizes of spatial units.
discvar	Name of continuous variable columns that need to be discretized. Noted that when <code>formula</code> has <code>discvar</code> , <code>data</code> must have these columns.
discnum	(optional) A vector of number of classes for discretization. Default is 3:22.
discmethod	(optional) A vector of methods for discretization, default is used <code>c("sd", "equal", "pretty", "quantile")</code> .
cores	(optional) A positive integer(default is 1). If <code>cores &gt; 1</code> , a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
increase_rate	(optional) The critical increase rate of the number of discretization. Default is 5%.
alpha	(optional) Specifies the size of confidence level. Default is 0.95.
...	(optional) Other arguments passed to <code>gd_bestunidisc()</code> .

## Details

Firstly, the OPGD model is executed for each data in the `datalist` (all significant Q statistic of each data are averaged to represent the spatial connection strength under this spatial unit), and then the `loess_optscale` function is used to select the optimal spatial analysis scale.

## Value

A list with `sesu`(size effects of spatial units) and `optsu`(optimal spatial unit).

## Author(s)

Wenbo Lv <[llyu.geosocial@gmail.com](mailto:llyu.geosocial@gmail.com)>

## References

Song, Y., Wang, J., Ge, Y. & Xu, C. (2020) An optimal parameters-based geographical detector model enhances geographic characteristics of explanatory variables for spatial heterogeneity analysis: Cases with different types of spatial data, *GIScience & Remote Sensing*, 57(5), 593-610. doi: 10.1080/15481603.2020.1760434.

## Examples

```
## Not run:
library(tidyverse)
fvcpath = "https://github.com/SpatLyu/rdevdata/raw/main/FVC.tif"
fvc = terra::rast(paste0("/vsicurl/", fvcpath))
fvc1000 = fvc %>%
  terra::as.data.frame(na.rm = T) %>%
  as_tibble()
fvc5000 = fvc %>%
  terra::aggregate(fact = 5) %>%
  terra::as.data.frame(na.rm = T) %>%
  as_tibble()
sesu_opgd(fvc ~ .,
           datalist = list(fvc1000, fvc5000),
           su = c(1000,5000),
           discvar = names(select(fvc5000,-c(fvc,lulc))),
           cores = 6)

## End(Not run)
```

**shuffle\_vector**      *randomly shuffling vector*

## Description

randomly shuffling vector

## Usage

```
shuffle_vector(x, shuffle_rate, seed = 123456789)
```

## Arguments

x	A vector.
shuffle_rate	The shuffling rate.
seed	(optional) Random seed number. Default is 123456789.

## Value

A shuffled vector.

## Examples

```
shuffle_vector(1:100, 0.15)
```

---

sim	<i>Simulation data.</i>
-----	-------------------------

---

## Description

Simulation data.

## Usage

```
sim
```

## Format

sim: A tibble with 80 rows and 6 variables, modified from IDSA package.

---

spade	<i>spatial association detector (SPADE) model</i>
-------	---

---

## Description

Function for spatial association detector (SPADE) model.

## Usage

```
spade(  
  formula,  
  data,  
  wt = NULL,  
  locations = NULL,  
  discnum = NULL,  
  discmethod = NULL,  
  cores = 6,  
  seed = 123456789,  
  permutations = 0,  
  ...  
)
```

## Arguments

formula	A formula of spatial association detector (SPADE) model.
data	A data.frame or tibble of observation data.
wt	(optional) The spatial weight matrix. When wt is not provided, must provide locations. And gdverse will use locations columns to construct spatial weight use inverse_distance_weight().

locations	(optional) The geospatial locations coordinate columns name which in data. Useful and must provided when wt is not provided. When wt is provided, locations is not need.
discnum	(optional) Number of multilevel discretization. Default will use 3:22.
discmethod	(optional) The discretization methods. Default all use quantile. When discmethod is robust use robust_disc(), others use st_unidisc()
cores	(optional) A positive integer(default is 6). If cores > 1, use parallel computation.
seed	(optional) Random number seed, default is 123456789.
permutations	(optional) The number of permutations for the PSD computation. Default is 0, which means no pseudo-p values are calculated.
...	(optional) Other arguments passed to st_unidisc() or robust_disc().

### Value

A list of the SPADE model result.

### Note

The columns in the locations part of data are only used to construct spatial weight matrix when wt is NULL, and are not considered as explanatory variables. If you need to include spatial locations as explanatory variables, build a spatial weight matrix ahead of time, leaving the locations parameter to NULL. The most recommended method is to explicitly specify all variables in formula instead of using .!

### Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

### References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE), International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

### Examples

```
## Not run:
library(sf)
usfi = read_sf(system.file('extdata/USFI_Xian.gpkg', package = 'gdverse')) |>
  dplyr::select(dplyr::all_of(c("NDVI", "BH", "SUHI")))
coord = usfi |>
  st_centroid() |>
  st_coordinates()
wt = inverse_distance_weight(coord[,1], coord[,2])
usfi = usfi |>
  dplyr::bind_cols(coord) |>
  st_drop_geometry()
spade('SUHI~.', data = usfi, locations = c('X', 'Y'), cores = 6)
spade('SUHI~.', data = usfi, wt = wt, locations = c('X', 'Y'),
      discmethod = c('sd', 'equal'), cores = 6)
```

---

```
## End(Not run)
```

---

**spd\_lesh***SHAP power of determinants (SPD)***Description**

Function for calculate SHAP power of determinants *SPD*.

**Usage**

```
spd_lesh(formula, data, cores = 1, ...)
```

**Arguments**

<code>formula</code>	A formula of calculate SHAP power of determinants <i>SPD</i> .
<code>data</code>	A data.frame or tibble of observation data.
<code>cores</code>	(optional) A positive integer(default is 1). If cores > 1, a 'parallel' package cluster with that many cores is created and used. You can also supply a cluster object.
...	(optional) Other arguments passed to <code>rpart_disc()</code> .

**Details**

The power of SHAP power of determinants formula is

$$\theta_{x_j}(S) = \sum_{s \in M \setminus \{x_j\}} \frac{|S|!(|M|-|S|-1)!}{|M|!} (v(S \cup \{x_j\}) - v(S)).$$

SHAP power of determinants (SPD) is the contribution of variable  $x_j$  to the power of determinants.

**Value**

A tibble with variable and its corresponding *SPD* value.

**Note**

The SHAP power of determinants (SPD) requires at least  $2^n - 1$  calculations when has  $n$  explanatory variables. When there are more than 10 explanatory variables, carefully consider the computational burden of this model. When there are a large number of explanatory variables, the data dimensionality reduction method can be used to ensure the trade-off between analysis results and calculation speed.

**Author(s)**

Wenbo Lv <luy.geosocial@gmail.com>

## References

Li, Y., Luo, P., Song, Y., Zhang, L., Qu, Y., & Hou, Z. (2023). A locally explained heterogeneity model for examining wetland disparity. International Journal of Digital Earth, 16(2), 4533–4552. <https://doi.org/10.1080/17538947.2023.2271883>

## Examples

```
## Not run:
data('ndvi')
g = spd_lesh(NDVIchange ~ ., data = ndvi, cores = 6)
g

## End(Not run)
```

**spvar**

*spatial variance*

## Description

Function for calculate inverse distance weight.

## Usage

```
spvar(yn, wtn)
```

## Arguments

- |     |  |
|-----|--|
| yn  | The numerical vector of a response variable. |
| wtn | The spatial weight matrix.                   |

## Details

The spatial variance formula is  $\Gamma = \frac{\sum_i \sum_{j \neq i} \omega_{ij} \frac{(y_i - y_j)^2}{2}}{\sum_i \sum_{j \neq i} \omega_{ij}}$

## Value

The spatial variance

## Author(s)

Wenbo Lv <[llyu.geosocial@gmail.com](mailto:llyu.geosocial@gmail.com)>

## References

Xuezhi Cang & Wei Luo (2018) Spatial association detector (SPADE),International Journal of Geographical Information Science, 32:10, 2055-2075, DOI: 10.1080/13658816.2018.1476693

## Examples

```
y = c(42,56,73)
wt1 = inverse_distance_weight(1:length(y),1:length(y))
wt2 = matrix(1,ncol = length(y),nrow = length(y))
diag(wt2) = 0
spvar(y,wt1)
spvar(y,wt2)
var(y)
```

---

st\_fuzzyoverlay      *spatial fuzzy overlay*

---

## Description

Function for spatial fuzzy overlay.

## Usage

```
st_fuzzyoverlay(formula, data, method = "and")
```

## Arguments

formula	A formula of spatial fuzzy overlay.
data	A data.frame or tibble of discretized data.
method	(optional) Overlay methods. When method is and, use min to do fuzzy overlay;and when method is or,use max to do fuzzy overlay. Default is and.

## Value

A spatial fuzzy overlay vector.

## Note

Independent variables in the data provided to st\_fuzzyoverlay() must be discretized variables, and dependent variables are continuous variables.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

## References

Yongze Song & Peng Wu (2021) An interactive detector for spatial associations, International Journal of Geographical Information Science, 35:8, 1676-1701, DOI:10.1080/13658816.2021.1882680

## Examples

```
data('sim')
sim = sim %>%
  dplyr::mutate(dplyr::across(4:6,\(.) st_unidisc(.x,4,"quantile")))
fo1 = st_fuzzyoverlay(y~xa+xb+xc,data = sim, method = 'and')
fo2 = st_fuzzyoverlay(y~xa+xb+xc,data = sim, method = 'or')
fo1
fo2
```

### st\_unidisc

*univariate discretization*

## Description

Function to classify univariate vector to interval,a wrapper of `classInt::classify_intervals()`.

## Usage

```
st_unidisc(x, k, method = "quantile", factor = FALSE, seed = 123456789, ...)
```

## Arguments

x	A continuous numerical variable.
k	(optional) Number of classes required, if missing, <code>grDevices::nclass.Sturges()</code> is used; see also the "dphi" and "headtails" styles for automatic choice of the number of classes. k must greater than 3 !
method	Chosen classify style: one of "fixed", "sd", "equal", "pretty", "quantile", "kmeans", "hclust", "bclust", "fisher", "jenks", "dphi", "headtails", "maximum", or "box". Default is quantile.
factor	(optional) Default is FALSE, if TRUE returns cols as a factor with intervals as labels rather than integers.
seed	(optional) Random seed number, default is 123456789. Setting random seed is useful when the sample size is greater than 3000(the default value for <code>largeN</code> ) and the data is discretized by sampling 10%(the default value for <code>samp_prop</code> ).
...	(optional) Other arguments passed to <code>classInt::classify_intervals()</code> , see <code>?classInt::classify_intervals()</code> .

## Value

A discrete vectors after being discretized.

## Author(s)

Wenbo Lv <llyu.geosocial@gmail.com>

**Examples**

```
xvar = c(22361, 9573, 4836, 5309, 10384, 4359, 11016, 4414, 3327, 3408,
       17816, 6909, 6936, 7990, 3758, 3569, 21965, 3605, 2181, 1892,
       2459, 2934, 6399, 8578, 8537, 4840, 12132, 3734, 4372, 9073,
       7508, 5203)
st_unidisc(xvar,k = 6,method = 'sd')
```

---

**weight\_assign**      *assign values by weight*

---

**Description**

assign values by weight

**Usage**

```
weight_assign(x, w, list = FALSE)
```

**Arguments**

x	A numeric value
w	A weight vector
list	(optional) Return list or not. if list is TRUE, return a list, otherwise return a vector. Default is FALSE.

**Value**

A numeric Vector.

**Examples**

```
weight_assign(0.875,1:3)
```

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